

Heat Transfer Enhancement in MCHS using Al_2O_3 /Water Nanofluid

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Abstract

In the present paper, Numerical simulation is performed to investigate the laminar force convection of Al_2O_3 /water Nanofluid in a flow channel with different constant heat flux 50, 90, 150 W/cm^2 respectively and two values of mass flow rate of fluid. The heat sources are placed on the bottom wall of channel which produces much thermal energy that must be discarded from the system. The remaining surfaces of channel are kept adiabatic to exchange energy between Nanofluid and heat sources. The effects of Reynolds number $Re < 1000$, the volume fraction of nanoparticles of nanofluid have the percentages of 0, 1, 3 and 5%. on the average heat transfer coefficient (h), pressure drop (ΔP), surface Nusselt number and wall temperature (T_w) are evaluated. The use of Nanofluid can produce an asymmetric velocity along the height of the channel. The results show that the wall temperature decreases remarkably as Re and volume of fraction increase. It is also observed that there is an enhancement of average heat transfer coefficient and it's observed also that the use of Nanofluid improves MCHS performance by reducing fin (conductive) thermal resistance.

Keywords: Nanofluid ; Laminar flow; Pressure drop; Heat transfer enhancement ; Forced Convection .

تحسين انتقال الحرارة في القنوات الميكروية باستخدام جسيمات النانوية الناتجة من خلط اوكسيد الالمنيوم مع الماء

في الدراسة المقدمة تم جراء محاكاة عددية لدراسة انتقال الحرارة بالحمل القسري لجريان طباقى لمائع (نانو) ناتج من خلط الماء مع جسيمات اوكسيد الالمنيوم يجري داخل قناة ميكروية مستطيلة الشكل محاطة بمادة السليكون الحراري وعرضه لفيض حراري ثابت وبمقادير مختلفة 50 ، 90 ، 150 واط / سنتيمتر المربع على التوالي مع نسبة تدفق من السائل النانوي وبمقدار 1×10^{-5} و 5.1×10^{-5} كغم بالثانية على التوالي. تم تسليط الفيض الحراري عند السطح السفلي للقناة . اما السطوح الباقية للقناة تبقى معزولة. تم دراسة اتاثير كل من سرعة الجريان للسائل ولأعداد رينولد اقل من 1000، والنسب الحجمية للجسيمات في الماء 0، 1، 3 و 5 % على معامل انتقال الحرارة بالحمل ، فرق الضغط ، عدد نوسيلت ودرجة حرارة الجدران . بينت النتائج المستنبطه من الدراسة ان استخدام الجسيمات تنتج سرعة لا متناظرة على طول ارتفاع القناة اضافة الى هبوط في درجة حرارة الجدار مع زياده السرعة والنسب الحجمية للجسيمات. كما بينت النتائج تحسين معامل انتقال الحرارة بالحمل من خلال انخفاض في المقاومة الحرارية للتوصيل الحراري.

الكلمات الدالة: المائع النانوي، جريان طباقى، انخفاض الضغط، تحسين انتقال الحرارة، الحمل القسري

Introduction

In last decade, primary research begins in the quest of using the nanoparticles in the various fields of applications. In the heat transfer problems values the quest for a good heat extraction in various ways of either using many fluids that have promising heat extraction efficiency. The maximum of a base fluid with Nano particle shows marked heat transfer enhancement^[1]. Further investigation regarding an increases in the surface area of the radiative /convective surfaces for which a micro channels being introduced in the problems of that transfer enhancement^[2].

As far as contribution of the friction factor and pressure drop for a laminar flow in the range up to 2000 Reynold number have a linearly variation in a micro chanel hydraulic geometry^[3,4].

Concerning the geometrical shape with regarding its aspect ratio to the hydraulic diameter where the friction factor found to have some dependence^[5,6,7 and 8], and this aspect ratios has no noticeable effect as far as the flow in laminar^[9].

The Nanofluid can its maintained its enhancement properties in the range of up to 5% of nanoparticles to the base fluid^[10]. While the channel geometrical shape affect the heat conductive properties by the geometrical size criterion and its volume proposed by the presence of thermal resistance^[11,12,13 and 14]

Gupta et al.^[15] studied fully developed laminar flow and heat transfer in equilateral triangular cross-sectional ducts with constant heat flux. Limited studies regarding the use nanofluids as coolants in micro and minichannel heat sinks exist in literature. Nguyen et al.^[16] have investigated the usage of nanofluids in cooling electronic devices with nanofluids as the coolant marked

reduction in the junction temperature was observed, especially at higher flow rates and higher particle loading percentage.

Micro channel cooling is a promising way to solve the cooling problem for computer chips. In micro channel cooling a fluid is flowing through a micro channel in close contact with the electronic chips. Due to the large area to volume ratio of the micro channel, the heat removal is larger than by conventional air cooling. Heat transfer by forced convection for gases is in the range 25-250 KW/m²^[17], whereas experimental micro channels with water have shown a heat flux of 500 KW/m²^[18].

The aim of this work is to study the heat transfer enhancement for Al₂O₃ nano particle with water of distinct intrinsic thermal properties in a rectangular micro channel that exposed to different heat flux 50, 90 and 150 W/cm² respectively that give surface temperature of near 80 degree. Two mass flow rate of 1 x10⁻⁵ and 5.1 x10⁻⁵ kg/sec.

Numerical Solution and Mathematical Modeling for the case study

In this case study a micro channel heat sink of silicon configured in the figure 1.a,b,c and the flowing nanofluid of Al₂O₃/ water in the micro channel of rectangular cross-sectional area. The assumed flow of the nanofluid in question has to have a laminar flow. This configuration of the heat sink of the fluid performs a 3D conjugate heat transfer in the nanofluid. The channel dimensions given in table.1

In this configuration the heat flux subjected from the base and both silicon fins in a uniform heat flux which is dissipated in the nanofluid coolant. In order to control the flow of

the fluid a forced flow in the micro duct with laminar flow being assumed of up to 1000 Reynold. Thus fluid at 20 C were supplied to the duct with two mass flow rate of 1×10^{-5} and 5.1×10^{-5} kg/sec and the heat flux assumed at 50,90 and 150 w/cm^2 exposed from the lower surface.

In order to get the requirements of the numerical solution, a discretization of the system of governing equations are given in appendix 1. A mesh generation in Gambit^[19] was performed as shown in Figure 2.a,b,c and table (2). These numbers were optimized after many attempts to have a study solution and reduction in the number of iteration required for convergence.

1. Governing equations.

The Microchannel heat exchanger (MCHE) considered in this case is shown schematically in Figure(1). Heat is transferred between the fluids through the sink wall separating them. Several assumptions were made on the operating conditions:

1. The MCHE operates under steady-state conditions with Constant heat flux and negligible radiation heat transfer.
2. The fluids remain in single phase along the channel and the flow is laminar.
3. Thermophysical properties of the fluids and MCHE material are temperature-independent.
4. Flow mis-distribution and external heat transfer effects are neglected.
5. The outer walls of the MCHE are considered insulated (adiabatic).

The system of equations with other parametric relations is in good processing with fluent Code^[20].

2. Thermo physical properties

The various thermal physical properties of Nanofluids can be evaluated as follows:

► Density and Viscosity

The base-fluid considered in this work is water. Thermo-physical properties were obtained as polynomial functions of temperature found some were else^[21] as :

$$\rho_w = -3.57 \times 10^{-3} T^2 + 1.88T + 753.2 \dots (1)$$

while the water viscosity is given by :

$$\mu_w = 2.591 \times 10^{-5} \times 10^{\frac{2383}{T-1432}} \dots (2)$$

The specific heat of water is considered constant at $C_{p_w} = 4200$. The effective density of the Nanofluid containing suspended particles can be evaluated through the following equation:

$$\rho_{nf} = \frac{\rho_{bf} V_{bf} + \rho_p V_p}{V_{bf} + V_p} = (1-\phi)\rho_{bf} + \phi\rho_p \dots (3)$$

For typical Nanofluids with Nanoparticles at a value of volume fraction less than 1%, a- minor change of less than 5% in the fluid density is expected. With respect to viscosity : the viscosity of mixture particles/fluid have two model invalued in calculation the Maxwell model which is introduced for sub millimetric size particles in suspension in fluid and that of Enstien Model for nano particles in suspension in fluid with volume fraction less than 0.01, where the surface interaction between particles and fluid being neglected. The Enstien Model^[22] expressed as :

$$\mu_{nf} = \mu_{bf}(1 + 2.5\phi) \dots (4)$$

However other correlated models for $\text{Al}_2\text{O}_3/\text{water}$ have been considered:

$$\mu_{nf} = (123\phi^2 + 7.3\phi + 1)\mu_f \dots [23] (5)$$

$$\mu_{nf} = (1 + 39.1\phi + 533.9\phi^2)\mu_f \dots [24] (6)$$

$$\mu_{nf} = (6.2\phi^2 + 2.5\phi + 1)\mu_f \dots [25] (7)$$

$$\mu_{nf} = (150\phi^2 + 2.5\phi + 1)\mu_f \dots [26] (8)$$

This correlation adapted for the present calculation as taking into consideration the size of the particles of less than 36 nm which can accommodate the agglomeration that can exist in real fluid under investigation.

Specific Heat

The specific heat of Nanofluid can be determined on assumption that a thermal equilibrium between the Nanoparticles and base fluid maintained as follows:

$$Cp_{nf} = \frac{(1-\phi)\rho_f Cp_f + \phi\rho_p Cp_p}{\rho_{nf}} \quad (9)$$

Using this relation a prediction of small decrement in specific heat for 3% Al₂O₃/water within a range of 7-8% to that of water. Due the size dependent that being noticed [26-29] a relation adapted of Yang and Zhang [31] :

$$(Cp)_{bf} = \frac{(1-\phi)(\rho Cp)_{bf} + \phi(\rho Cp)_p}{(1-\phi)\rho_{bf} + \phi\rho_p} \quad (10)$$

Thermal Conductivity

The effective thermal conductivity of Nanofluids based on an empirical model of Maxwell [31] on assumption that a spherical particles shape dispersed a supporting field:

$$\frac{k_{nf}}{k_f} = 1 + \frac{3(\alpha-1)\phi}{(\alpha+2) - (\alpha-1)\phi}, \quad \alpha = \frac{k_p}{k_f} \quad (11)$$

And $k_{nf} = k_{bf}(4.97\phi^2 + 2.7\phi + 1)$

for Water / γ -Al₂O₃

For two other effecting physical parameter the shape of the particles and the effect of the particle motion in the fluid. A brownian type random movement being introduced by Hamilton and Crosser [32]. The Maxwell correlate becomes:

$$\frac{k_{nf}}{k_f} = \frac{[k_p + (n-1)k_f - (n-1)\phi(k_f - k_p)]}{[k_p + (n-1)k_f + \phi(k_f - k_p)]} \quad (12)$$

Where the parameter n is the ‘shape factor’ defined as : $n = \frac{3}{\psi}$, where ψ

called the (Sphericity), is defined as the ratio of the surface area of the sphere to that of the particle for the same volume. For spherical particles $\psi = 1$, and for the cylinders $\psi = 0.5$. Jang and Choi [33] found that the Brownian motion of Nanoparticles at the molecular and Nano scale level is a key mechanism governing the thermal behavior of Nanofluids .

3. Pure and Nanofluid Temperature

In The Nanofluid and pure fluid cooling MCHS, the energy absorbed by the working fluid can be written as :

$$Q_{nf} = (\rho Cp)_{nf} \dot{V}_{nf} (T_{nfo} - T_{nfi}) = (\rho Cp)_{nf} \dot{V}_{nf} \Delta T_{nf} \quad (13)$$

$$Q_f = (\rho Cp)_f \dot{V}_f (T_{fo} - T_{fi}) = (\rho Cp)_f \dot{V}_f \Delta T_f \quad (14)$$

noting that the thermal capacity of the Nanofluid is usually smaller than that for the pure fluid because of the low specific heat of Nanoparticles .

From Newton’s law of cooling, the local heat transfer coefficient for both Nanofluid and pure fluid cooled MCHS can be written as:

$$q'' = h_{nf}(x)(T_{snf}(x) - T_{nf}(x)) = h_f(x)(T_{sf}(x) - T_f(x)) \quad (15)$$

$$h_{nf}(x) = \frac{q''}{(T_{snf}(x) - T_{nf}(x))}, h_f(x) = \frac{q''}{(T_{sf}(x) - T_f(x))} \quad (16)$$

in order to established a heat transfer enhancement by the Nanofluid If the , $h_{nf}(x) > h_f(x)$ and $Q_{nf} > Q_f$ conditionally $\dot{V}_{nf} = \dot{V}_f$ and $T_{nfi} = T_{fi}$, we observed that :

$$(T_{nfo} - T_{nfi}) > (T_{fo} - T_{fi}) \dots\dots\dots(17)$$

$$(T_{snf}(x) - T_{nf}(x)) < (T_{sf}(x) - T_f(x)) \quad (18)$$

by Combining Eqs. (27) and (28), it can be found that :

$$T_{snf}(x) < T_{sf}(x) \dots\dots\dots(19)$$

This result indicates that Nanofluid can cool MCHS better than pure fluid.

Results and Discussions

The calculation being carried by using the FLUENT code (Ansys 12) and the mesh that has been established as mentioned earlier. These calculations established for two mass flow rates that maintained a laminar flow through the channel. Then three heat flux imposed on the channel accordingly there mixture of nanofluid and pure water being used.

The temperature distribution across the cross sectional area and respectively with its length has been estimated as shown in Figure (3) to (8) for are the temperature contours of the outlet of the channel a mentioned conditions. While the profile along the channel presented in Figure (9) and (10) and table (4). As noted on each the related condition.

The contacted results from the contours of the temperature distribution in highest in contact with channel wall and concaving toward the center of the channel, while the temperature profile along the channel decreasing with respect to either increasing nanofluid concentration or the increasing velocity. Then the velocity profile for each at the exit shown in figures (11-16).

Concerning the heat transfer coefficient a three regions along the channel being noticed for the pure water to that of the mixture nanofluids so that a rapid slope ends at 1 mm for water and the mixtures but the intermediate range for water

ends at 6 mm while the mixtures ends at 7 mm, furthermore length being steady state meaning a better heat transfer coefficient for the mixtures from that of pure water Figure(17). similarly the Nusselt number confirm this type of behavior but Nusselt resolve very clearly the transfer enhancement from the lower concentration to the higher one as shown in figure 18a,b,c. Never the less, to confirm this results with ^[34] shows that a close similarity in the result concerning Nusselt number Figure 19. In comparing to heat flux with both Nusselt number and Reynold number shows the higher the heat flux have its highest and a linearly variation with the increasing of both number and shows a lower value for a lower heat flux as given in figure(20).

Conclusions

The simulated flow inside a micro channel for Al₂O₃/water mixture with different concentration to conduct heat flux exposed from bottom side of the channel to be constant at 50 W/cm², 90w/cm² and 200 W/cm². The flow of the fluid assumed laminar in range of less than 1000 Reynold number, for concentrations of 1%, 3% and 5%. The outlet flow temperatures obtained from the calculations for both of flow rate which is mentioned previous and heat fluxes (50 W/cm² and 90 W/cm²) is less than 80 degree centigrade while greater than 80 degree centigrade at 150 W/cm² for the same conditions. Also From the review of the Nanofluid thermal conductivity study in the literatures, it is seen that there is a significant discrepancy in experimental data. This discrepancy may be due to some specific parameters of Nanofluids such is clustering of Nanoparticles, particle size distribution of Nanoparticles, duration and severity of ultrasonic vibration applied to the

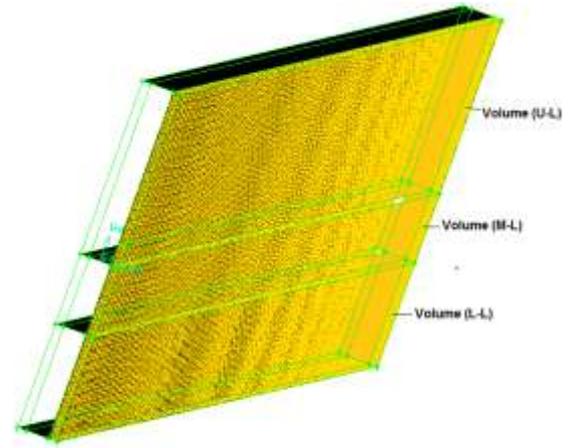
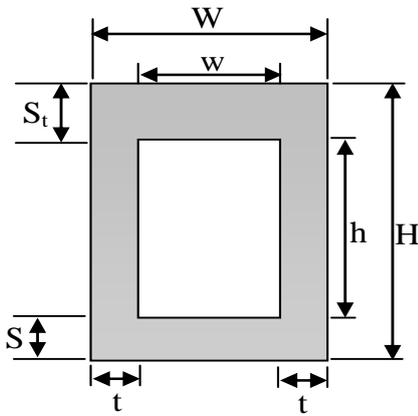
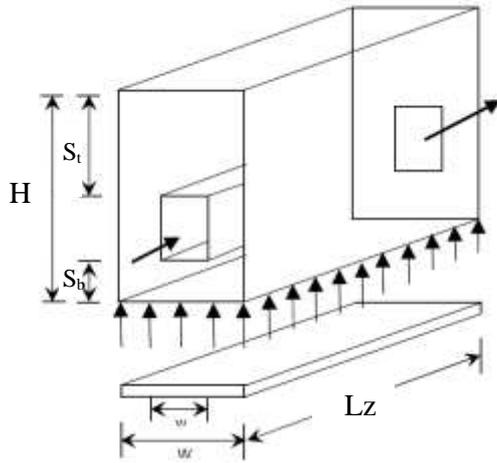
Nanofluid, and pH value of the Nanofluid.

The analysis performed, provides a-fundamental understanding of the combined flow and conjugate convection–conduction heat transfer in the three-dimensional Microchannel heat sink. Therefore, the results of the analysis as well as the conclusions can be considered as quite general and applicable to any three-dimensional conjugate heat transfer problems.

References

- 1- G. Roy, S.J. Palm and C.T. Nguyen, "Heat transfer and fluid flow of Nanofluids in laminar radial flow cooling," *Journal of Thermal Science*, 2005, Vol. 14, 4, 362-367,.
- 2- Tuckerman, D.B. and Pease, R.F.W., "High-performance heat sinking for VLSI", *IEEE Electron Device Letters* 1981.
- 3- Wu, P. and Little, W.A., "Measurement of friction factors for the flow of gases in very fine channels used for micro miniature Joule-Thomson refrigerators", *Cryogenics* .
- 4- Liu, D. and Garimella, S.V., "Investigation of liquid flow in micro channels, *AIAA Journal of Thermo physics and Heat Transfer*", 2004, Vol. 18, p. 65–72.
- 5- Jung, J., Oh, H. and Kwak, H. Forced convective heat transfer of Nanofluids in Microchannels. *International Journal of Heat and Mass Transfer*. 2009, 52, 466 – 472.
- 6- Choi, S.B., Barron, R.F., and Warrington, R.O., Fluid flow and heat transfer in Micro tubes, *Micromechanical Sensors, Actuators, and Systems*, ASME DSC, 1991, Vol. 32, 123–134 .
- 7- Rahman, m.m.and gui. Experimental measurements of fluid flow and heat transfer in micro scale cooling passage in a chip substrate.
- 8- Peng, X.F. and Peterson, G.P., Convective heat transfer and flow friction for water flow in micro channel structures. *Int. J. Heat Mass Transfer*. 1996, 39 12, 2599–2608 .
- 9- Judy, J., Maynes, D., and Webb, B.W., Characterization of frictional pressure drop for liquid flows through micro channels, *International Journal of Heat and Mass Transfer*, 2002 .
- 10- Nguyen, C., Desgranges, F., Roy, G., Galanis, N., Maré, T., Boucher, S., and Angue Mintsa, H., "Temperature and Particle-Size Dependent Viscosity Data for Water-Based Nanofluids - Hysteresis Phenomenon," *Int. J. Heat Fluid Fl.*, 2007. 28(6), 1492-1506 .
- 11- A.G. Fedorov, R. Viskanta, Three-dimensional conjugate heat transfer in the Micro channel heat sink for electronic packaging, *Int. J. Heat Mass Transfer*, 2000. 43 (3).
- 12- Shah RK: Laminar flow friction & forced convection heat transfer in ducts of arbitrary geometry. *Int J Heat Mass Transfer* 1975, 18:849-862 .
- 13- Shah RK, London AL: Laminar Flow Forced Convection in Ducts New York: Academic Press Inc; 1978 .
- 14- J. Driker J.P. Meyer, " Thermal characterization of embedded heat Spreading layer in rectangular heat generating electronic modules " , *International Journal of heat and mass transfer*, 2009, Vol.52 , 1374-1384.
15. Gupta RV, Geyer PE, Fletcher DF, Haynes BS: Thermohydraulic performance of a periodic trapezoidal channel with a triangular cross-

- section. *Int J Heat Mass Trans.* 2008, 51:2925-2929.
- 16 Nguyen, C., Desgranges, F., Roy, G., Galanis, N., Maré, T., Boucher, S., and Angue Mintsa, H., "Temperature and Particle-Size Dependent Viscosity Data for Water-Based Nanofluids - Hysteresis Phenomenon," *Int. J. Heat Fluid Fl.* 2007,28(6), 1492-1506.
 17. Incropera, F.P.& DeWitt, D. F "Fundamentals of heat and mass transfer", Wiley 2001.
 18. Kuan, W. K. & Kandlikar, S. G.. "Experimental study and model on critical heat flux of refrigerant123 and water in microchannels". *Journal of heat transfer*, 2008. 130, 034503
 - 19- Fluent Inc. , Gambit version 6 manuals , centerra resource park , 10 Cavendish Court , Lebanon , New Hampshire, USA, 2001 (www.fluent.com) .
 - 20- Fluent Inc. , Fluent Version 12.0.16 Manuals, Centerra Resource Park , 10 Cavendish Court, Lebanon, New Hampshire,USA,2001, www.fluent.com.
 - 21- Kays W, Crawford M, Weigand B: *Convective Heat and Mass Transport.* 4 edition. Singapore: MacGraw Hill; 2005.
 - 22- Einstein, A., "A New Determination of the Molecular Dimensions," *Ann. Phys.* 1906 324(2), 289-306.
 - 23- X Wang, X Xu and S U S Choi, J. *Thermophys. Heat Transfer* 13(4), 474, 1999.
 - 24- B C Pak and Y I Cho, *Expt. Heat Transfer.* 1998, 11, 151.
 - 25- Batchelor, G. K., 1977, "The Effect of Brownian Motion on the Bulk Stress in a Suspension of Spherical Particles," *J. Fluid Mech.*, 83(1), pp. 97-117.
 - 26- B.C. Pak, Y.I. Cho, Hydrodynamic and heat transfer study of dispersed fluids with submicron metallic oxide particles, *Experimental Heat Transfer* 11 (1998) 151–170.
 - 27- S.E.B. Maiga, C.T. Nguyen, N. Galanis, G. Roy, Heat transfer behaviours of nanofluids in a uniformly heated tube, *Superlattices Microstructures* 35 (2004) 543–557.
 - 28- S.J. Palm, G. Roy, C.T. Nguyen, Heat transfer enhancement with the use of nanofluids in radial flow cooling systems considering temperature dependent properties, *Applied Thermal Engineering* 26 (2006) 2209–2218.
 - 29- S.K. Das, S.U.S. Choi, W. Yu, T. Pradeep, *Nanofluids science and technology*, John Wiley & Sons, Hoboken NJ, 2008.
 - 30- Yang, Y., Zhang, Z.G., Grulke, E.A., Anderson, W.B., Wu, G.F. "Heat transfer properties of nanoparticles-in-fluid dispersions (nanofluids) in laminar flow". *Int. J. Heat Mass Transfer*, 2005, 48, 1107-1116
 - 31- J C Maxwell , *A treatise on electricity and magnetism* , 2nd Ed . Clarendon Press, Oxford, UK, 1881, vol. 1, p. 440.
 - 32- R L Hamilton and O K Crosser , *Industrial and Engineering Chemistry Fundamentals* 1(3), 187 (1962) .
 - 33- S P Jang and S U S Choi , *Appl . Phys. Lett.* 84(21) , 4316 (2004) .
 - 34- AMRITRAJ BHANJA , " Numerical solution of three dimensional conjugate heat transfer in a Microchannel heat sink and CFD analysis " NATIONAL INSTITUTE OF TECHNOLOGY ROURKELA-769008 (2009) .



Figure(2) Schematic diagram of Single Microchannel in GAMBIT.

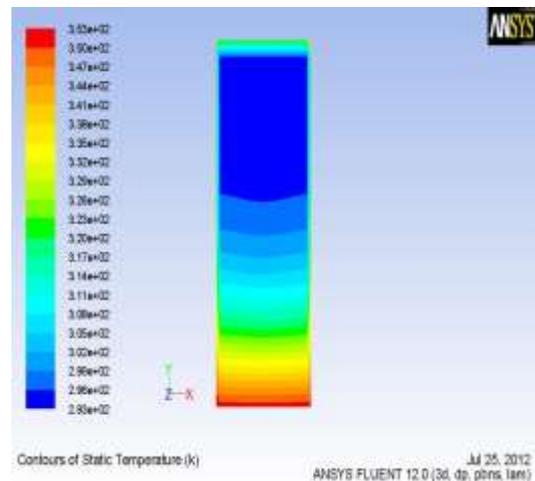
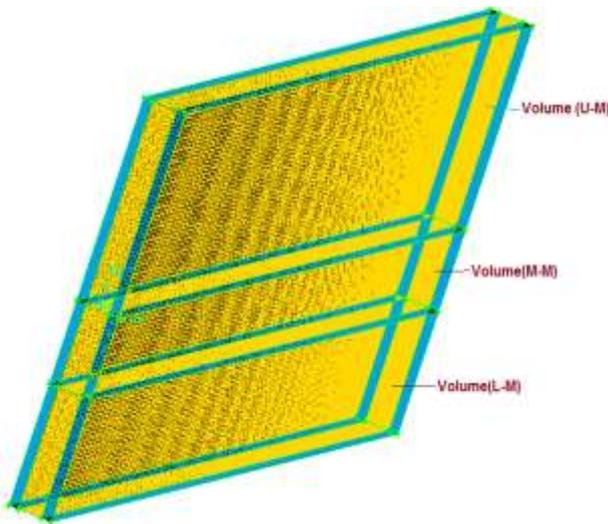
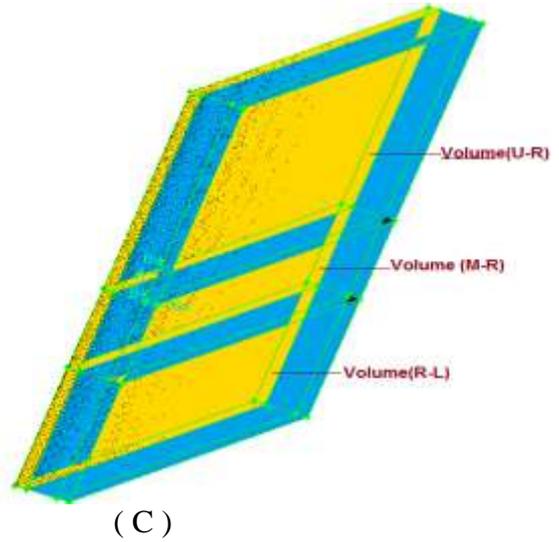


Fig. 3 Temperature contour of Outlet at $\phi=0\%$ and at $50W/cm^2$, $\dot{m}=1 \times 10^{-5} kg/s$.

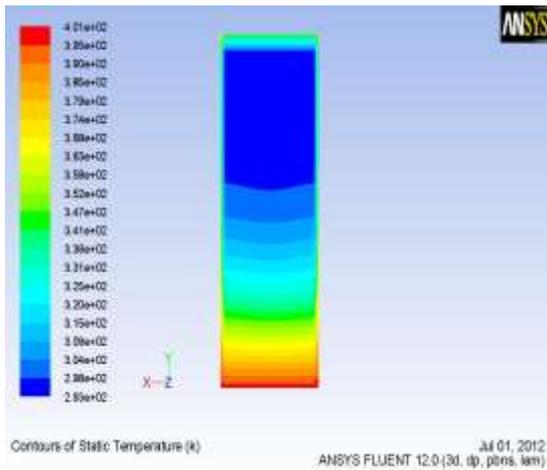


Fig. 4 Temperature contour of Outlet at $\Phi=0\%$ and at $90W/cm^2$, $\dot{m}=1 \times 10^{-5} kg/s$

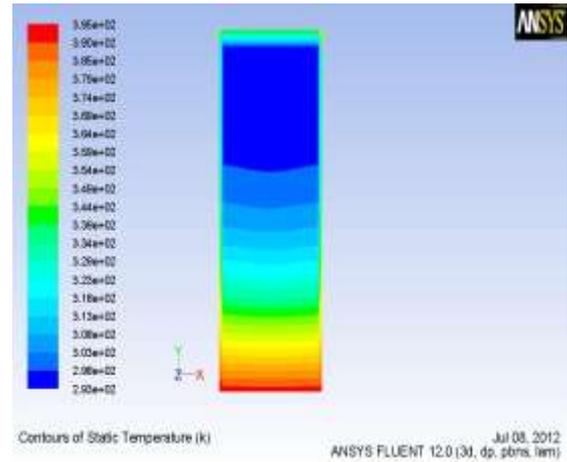


Fig. 7 Temperature contour of Outlet at $\Phi=5\%$ and at $90W/cm^2$, $\dot{m}=1 \times 10^{-5} Kg/s$.

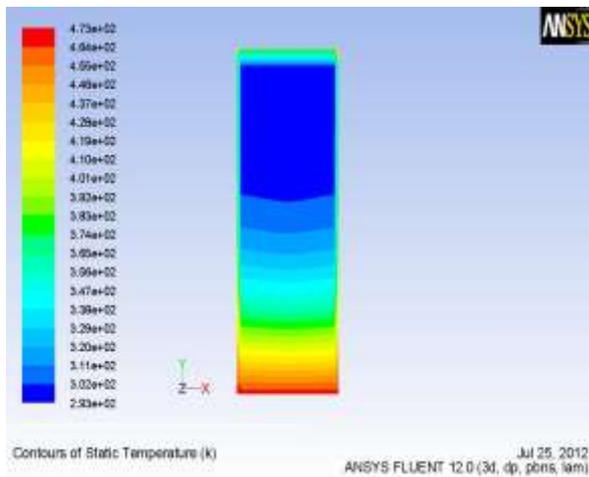


Fig. 5 Temperature contour of outlet at $\Phi=0\%$ and at $150w/cm^2$, $\dot{m}=1 \times 10^{-5} kg/s$.

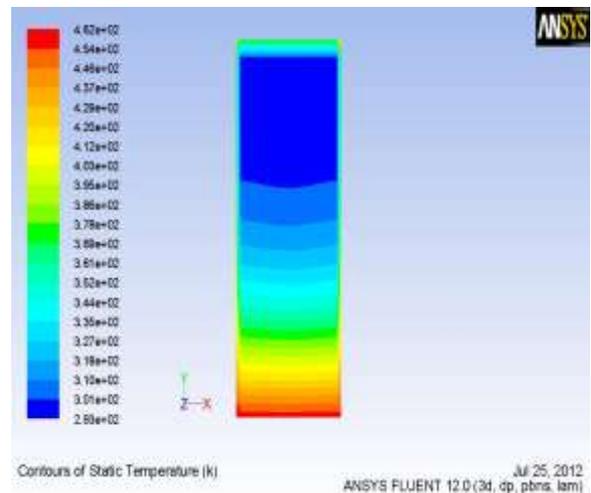


Fig. 8 Temperature contour of outlet at $\Phi=5\%$ and at $150w/cm^2$, $\dot{m}=1 \times 10^{-5} kg/s$.

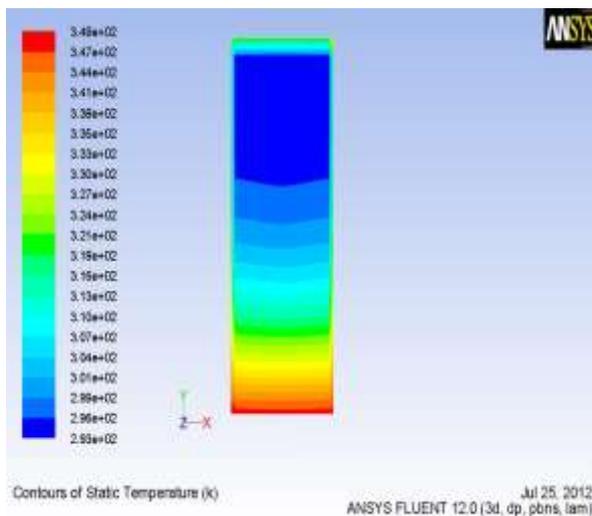


Fig. 6 Temperature contour of Outlet at $\Phi=5\%$ and at $50w/cm^2$, $\dot{m}=1 \times 10^{-5} kg/s$.

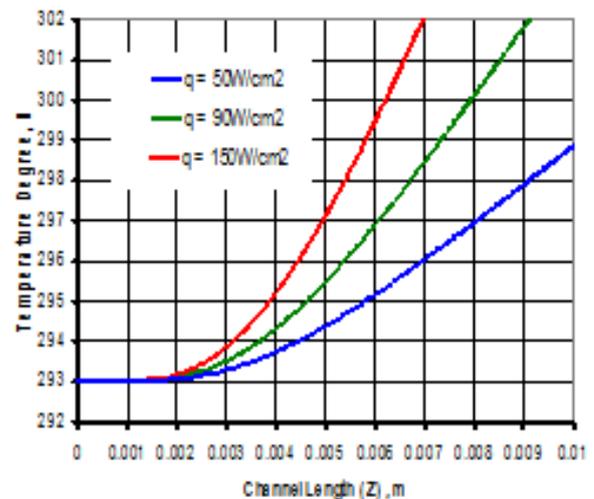


Fig. 9 Temperature profile of fluid at 5% Alumina, $\dot{m}=1.10 \times 10^{-5} kg/s$.

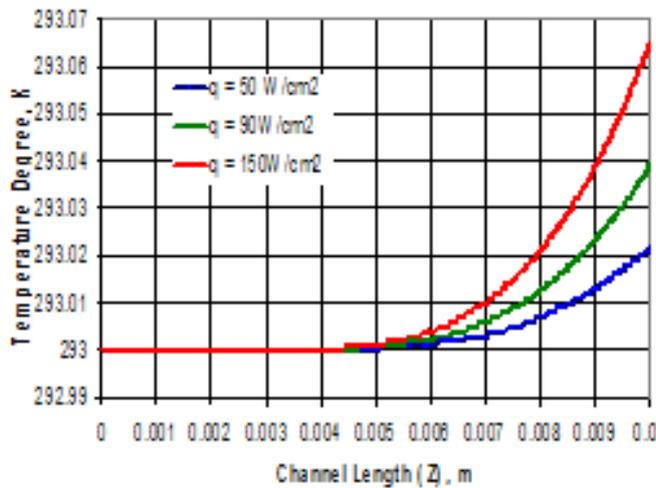


Fig. 10 Temperature profile of fluid at $\phi = 5\%$ Alumina, $\dot{m} = 5.12 \times 10^{-5} \text{ kg/s}$.

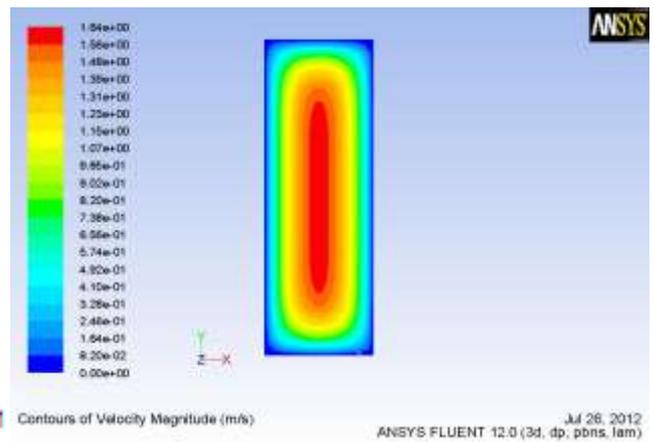


Fig. 13 Velocity contour of Outlet at $V = 0\%$ and at 90 W/cm^2 , $\dot{m} = 1 \times 10^{-5} \text{ kg/s}$.

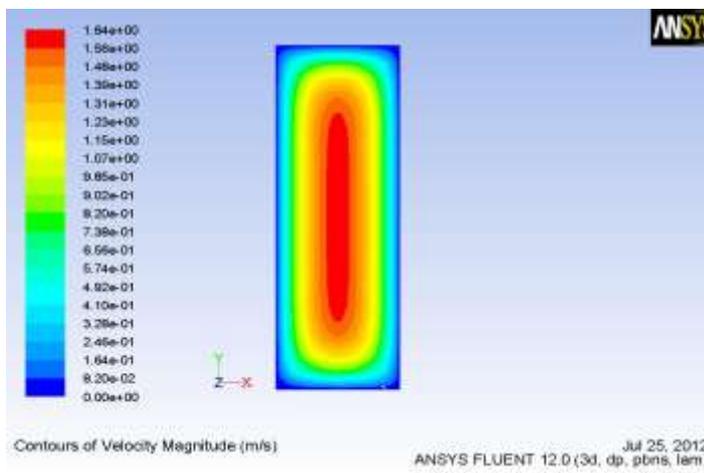


Fig. 11 Velocity contour of outlet at $\phi = 0\%$ and at 50 W/cm^2 , $\dot{m} = 1 \times 10^{-5} \text{ kg/s}$.

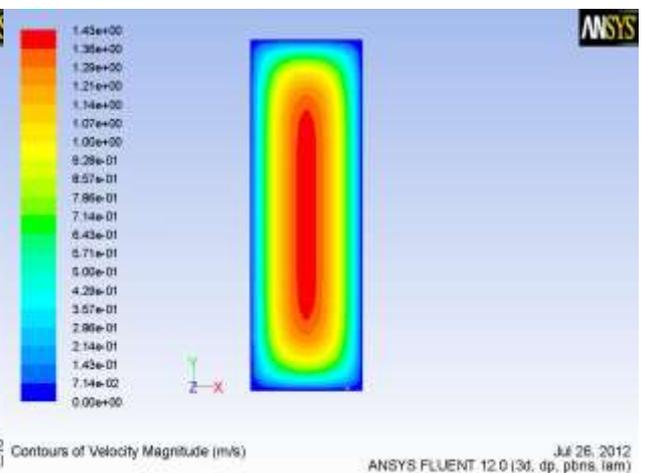


Fig. 14 Velocity contour of Outlet at $\phi = 5\%$ and at 90 W/cm^2 , $\dot{m} = 1 \times 10^{-5} \text{ kg/s}$.

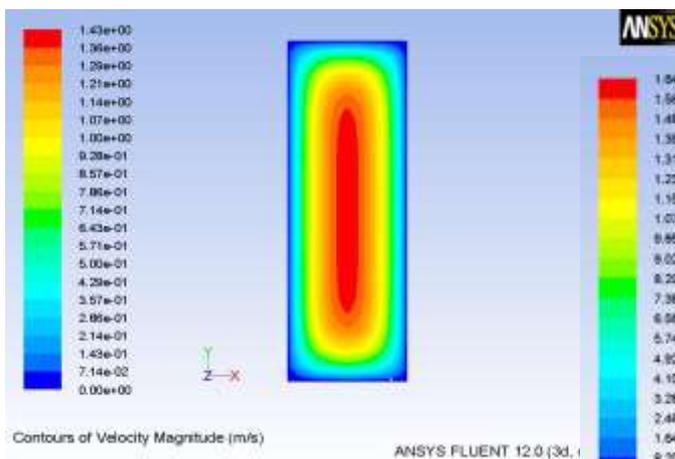


Fig. 12 Velocity contour of Outlet at $\phi = 5\%$ and at 50 W/cm^2 , $\dot{m} = 1 \times 10^{-5} \text{ kg/s}$.

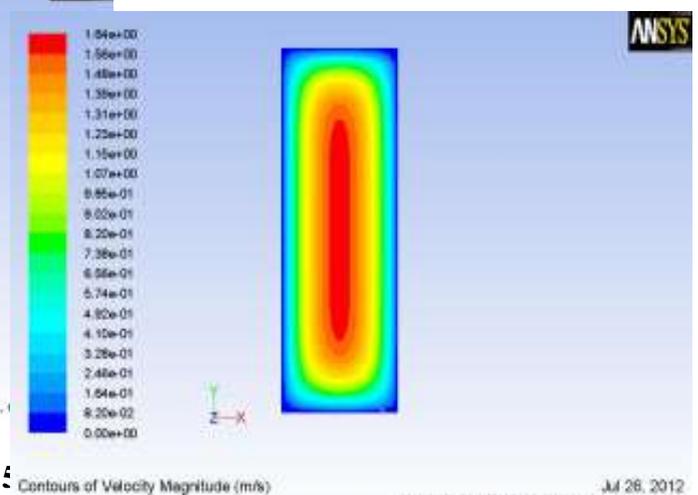


Fig. 15 Velocity contour of Outlet at $\phi = 0\%$ and at 150 W/cm^2 , $\dot{m} = 1 \times 10^{-5} \text{ kg/s}$.

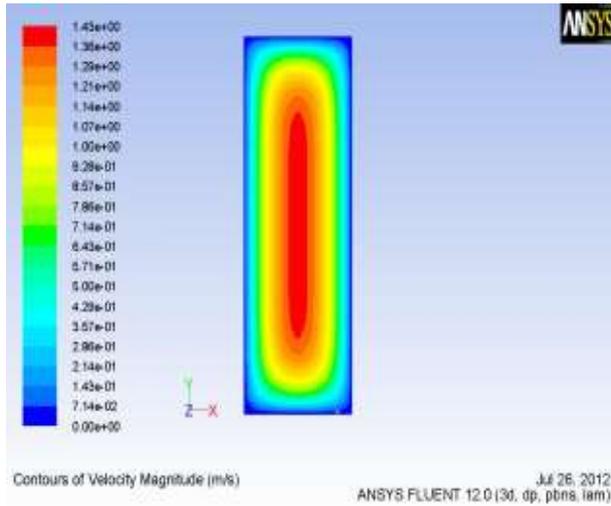


Fig. 16 Velocity contour of Outlet at $\Phi= 5\%$ and at 150w/cm^2 , $\dot{m}=1\times 10^{-5}\text{kg/s}$.

Table (1): Dimensions of the of the designed cooling model

W	100 μm
w	57 μm
H	900 μm
h	180 μm
t	21.5 μm
S_t	450 μm
S_b	270 μm
L_z	10000 μm
D_h	86 μm

Table(2).Volume and Node distribution

Volume	L-L	L-M	L-R	M-M	M-R
Node	43416	188136	43416	109746	25326
Element	35000	175000	35000	100000	20000
Volume	M-L	U-L	U-M	U-R	
Node	25326	61506	266526	61506	
Element	20000	50000	250000	50000	

Table (3).Estimate Parameters for Nanofluid Concentration

$\dot{m}=1\times 10^{-5}\text{kg/s}$	Heat Flux=50 w/cm^2		
property	$\Phi=0$	$\Phi=3$	$\Phi=5$
Temp.(K)	353	351	349
Re	83.57	62.83	49.95
V(m/sec)	0.9764	0.8945	0.8482

$\dot{m}=5.21\times 10^{-5}\text{kg/s}$	Heat Flux=50 w/cm^2		
property	$\Phi=0$	$\Phi=3$	$\Phi=5$

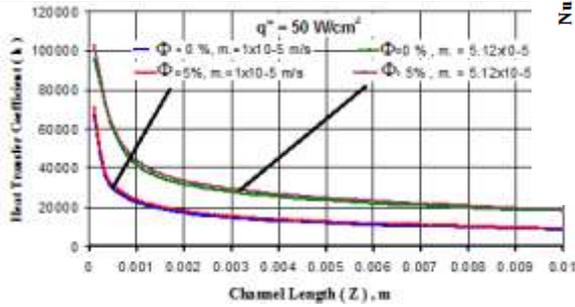
Temp.(K)	325	324	323
Re	427.9	321.7	8255.
V(m/sec)	5	4.58	4.34

$\dot{m}=1 \times 10^{-5} \text{ kg/s}$	Heat Flux=90 w/cm ²		
property	$\Phi=0$	$\Phi=3$	$\Phi=5$
Temp.(K)	401	397	395
Re	83.57	62.83	49.95
V(m/sec)	0.9764	0.8945	0.8482

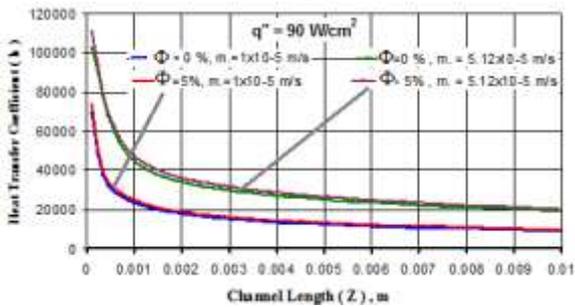
$\dot{m}=5.12 \times 10^{-5} \text{ kg/s}$	Heat Flux=90 w/cm ²		
property	$\Phi=0$	$\Phi=3$	$\Phi=5$
Temp.(K)	350	348	347
Re	427.9	321.7	255.
V(m/sec)	5	4.58	4.31

$\dot{m}=5.12 \times 10^{-5} \text{ kg/s}$	Heat Flux=150 w/cm ²		
property	$\Phi=0$	$\Phi=3$	$\Phi=5$
Temp.(K)	388	385	383
Re	427.	321.	255.
V(m/sec)	5	4.5	4.3

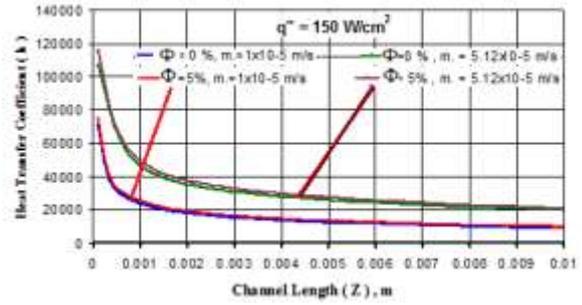
$\dot{m}=1.0 \times 10^{-5} \text{ kg/s}$	Heat Flux=150 w/cm ²		
Property	$\Phi=0$	$\Phi=3$	$\Phi=5$
Temp.(K)	473	467	462
Re	83.5	62.83	49.9
V(m/sec)	0.97	0.89	0.85



(a)

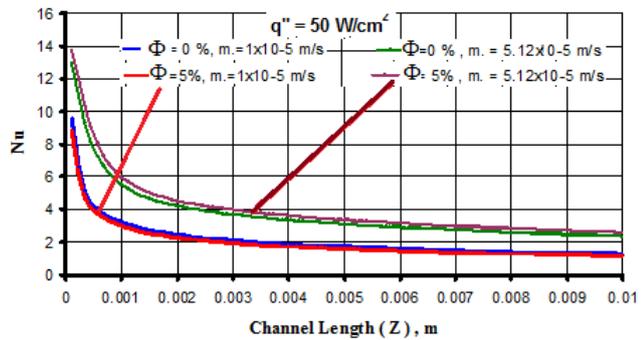


(b)

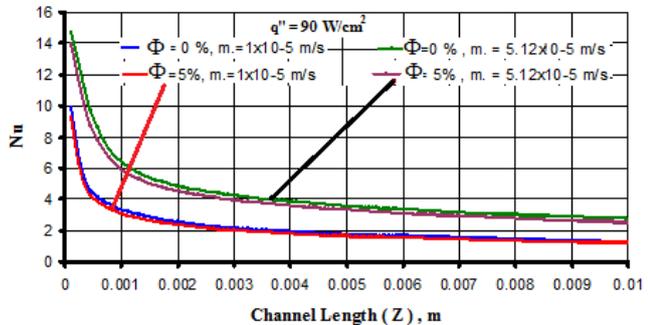


(c)

Fig. 17 Heat transfer coefficient profile along Microchannel with different at flux at different mass flow



(a)



(b)

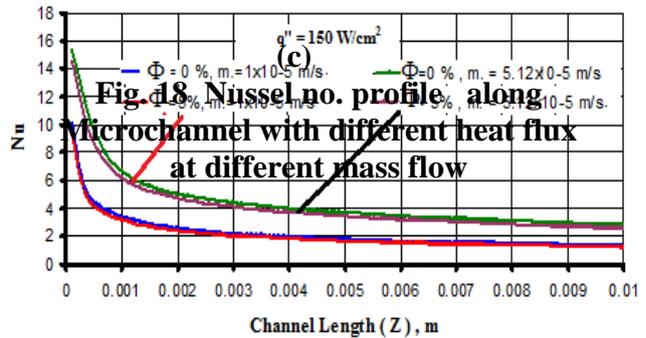


Fig. 18 Nussel no. profile along Microchannel with different heat flux at different mass flow

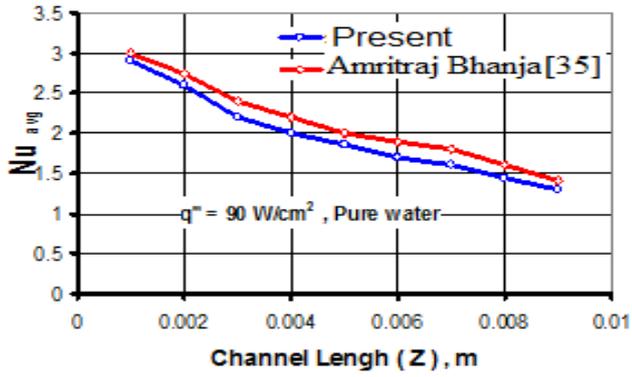


Fig. 19 Comparison of Nusselt Number profile along Micro channel

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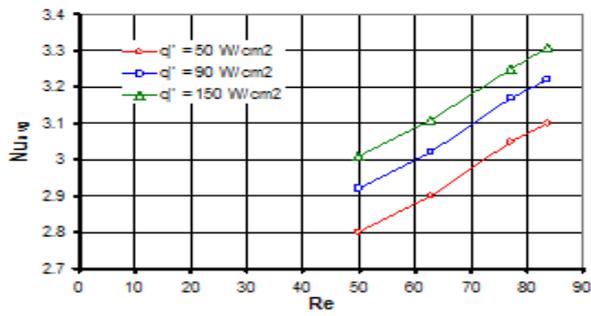


Fig. 20 Variation of average Nu with Re at different heat flux and

$$\dot{m} = 1 \times 10^{-5} \text{ kg/s} .$$