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# The Performance Prediction of The Mixed Convection In an Inclined Circular Tube Filled Porous Media Based on an Intelligent Control

## Keywords:

Mixed convection  
porous media  
inclined circular tube  
artificial neural network thermal  
performance

## ABSTRACT

The porous media has a significant impact on the heat transfer and storage properties. The present study focuses on the heat transfer of the mixed convection through a circular tube that filled with a porous media at different angles using a neural network. An experiment had been performed for the Rayleigh number range from 108.54 to 907.73 and the Peclet number range 30.3.-510 using three tests for the heat flux. The result shows the mean relative error about 7.913% and the coloration coefficient ( $R^2$ ) Is 99.18% for the train data. The mean relative error about 6.641% and the  $R^2$  is 99.46%, for the test data. The results showed that effectiveness of ANN in the predicted thermal performance in thermal engineering applications such as heat transfer modeling using porous media with airflow.

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تنبؤ أداء الحمل المختلط في انبوب دائري مائل مملوء بوسط مسامي قائم على تحكم ذكي وبيانات مختبرية

موسى مصطفى ويس / قسم الوقود والطاقة / الكلية التقنية / الجامعة التقنية الشمالية / كركوك / العراق

### الخلاصة :

الايوساط المسامية لها تأثير كبير على نقل الحرارة وخصائص التخزين. تركز الدراسة الحالية على انتقال الحرارة بالحمل المختلط عبر أنبوب دائري مملوء بالوسائط المسامية بزوايا مختلفة وذلك باستخدام شبكة عصبية. استخدمت البيانات الحقيقية في النتائج التجريبية. تم إجراء هذه التجارب لمجموعة أرقام رايلي ضمن المدى من 108.54 إلى 907.73 ورقم بكلت من 30.3 إلى 510 وباستخدام ثلاثة اختبارات للفيض الحراري. أظهرت النتائج بان معدل الخطأ النسبي كانت حوالي 7.913% ومعامل التلوين كانت ( $R^2$ ) 99.18% لبيانات التدريب. اما الخطأ النسبي قدر بحوالي 6.641% و ( $R^2$ ) 99.46% لبيانات الاختبار. حيث أظهرت النتائج فعالية ANN في التنبؤ بالأداء الحراري في تطبيقات الهندسة الحرارية مثل نمذجة نقل الحرارة باستخدام الوسائط المسامية مع تدفق الهواء.

الكلمات الدالة: الحمل المختلط، وسط مسامي، انبوب دائري مائل، شبكة اعصاب الصناعية، الاداء الحراري

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**Nomenclature**

$A_s$	Surface area ( $m^2$ )
$c_{p,f}$	Specific heat of the air ( $J/kg\ K$ )
$D$	Outside diameter (m)
$d_p$	Grain diameter (m)
$g$	Gravity acceleration ( $9.81\ m/s^2$ )
$Gr_z$	Grashof number
$h_z$	Local convection heat transfer ( $W/m^2\ ^\circ C$ )
$I$	current (A)
$K$	permeability ( $m^2$ )
$k_f$	thermal conductivity ( $W/m\ ^\circ C$ )
$l$	tube length (m)
$\dot{m}$	mass flow rate ( $kg/s$ )
$Nu_z$	Nusselt number
$Pe$	Peclet number
$Ra$	Rayleigh number
$Re$	Reynolds number
$Q$	power input (W)
$q$	Heat Transfer rate (W)
$q_w$	Heat flux ( $W/m^2$ )
$T_{in}$	inlet temperature ( $^\circ C$ )
$T_{out}$	outlet temperature ( $^\circ C$ )
$u$	air velocity ( $m/s$ )
$V$	supplied Voltage (V)
<b>Greek symbols</b>	
$\varepsilon$	Porosity
$\mu_f$	dynamic viscosity ( $N/m.s$ ) or $pas.sec$
$\rho_f$	density ( $kg/m^3$ )

**1.Introduction**

Researches had been directed in the last three centuries, especially after the increase of the demand for the energy in the world to attract work in two these areas are firstly looking for new alternatives to fossil energy, such as renewable energy and environment-friends. Second, to rationalize energy consumption by improving the performance of the thermal systems by looking for catalysts that lead to increase the heat transfer of these systems, such as the porous media in both types of a stuffed layer and fluidized bed [1-4]. Pu et al. [5]. Experiments were conducted on two regimes of convection heat transfer (laminar and turbulent) in a vertical channel with non-uniform heating of the two opposite walls and working conditions in the range of  $700 < Ra < 1500$  and  $2 < Pe < 2200$  and the measured temperature distribution in the vertical packed channel indicates a secondary thermal cell within it. The correlation relation for the Nusselt number was obtained in terms of the number of Peclet and Rayleigh of the experimental data and plot their relationship. Three

convection regimes have been noticed; forced convection  $Ra/Pe < 1$ , mixed convection  $1 < Ra/Pe < 105$  and natural convection  $105 < Ra/Pe$ . Many researchers study the mixed convection numerically [6-8], and experimental [9,10]

In many engineering applications, the artificial meshes had been used as it offer better and more logical solutions [11]. A feed-forward back propagation ANN was used to analyse in both numerical and experimental studies of heat transfers in the two-phases change process in an around the finned pipe. The average relative error in the experiment was about 5.58% while the numerical model ended with 14.99%. Fadare and Fatona [12] studied ANN in four kinds of exchanger models such as staggered multi-row, multi-column, cross-flow, and tube to a tube, the results were compared with the experimental data. Results showed that the relative error was less than 4% and 1% for testing and training data. Islamoglu and Kurt [13] used the ANN model to analyse the heat transfer rate of the corrugated channel. Results showed that the relative error between experimental and ANN results was less than 4%.

This study focused on the capability of ANN for heat transfer analysis in the circular tube filled with porous media horizontal and inclined with different angles as well as change the heat flux.

**3.Experimental Setup**

Experiments on convective heat transfer were carried out using the rig as shown in Fig.1, which consists of a circular copper tube of 45 and 47 mm inner and outer diameter respectively, 850mm length, it was filled with porous media and tube surface heated with a constant heat flux at different positions of the tube, starting from the horizontal and changing the angle to have different values  $30^\circ$ ,  $45^\circ$ ,  $60^\circ$ , respectively. The heated tube length about 800 mm and it was packed with glass balls of 5mm diameter of thermal conductivity of  $0.81\ W/m^\circ C$ . 48 thermocouples type T were used to measure temperature in the test tube. These thermocouples are fixed as; two thermocouples are allocated to measure the air inlet temperature and output and the rest were fixed with three thermocouples groups for each location in the tube. The outer surface of the tube is heated electrically using a 28-m of  $0.1\ \Omega$  electrical resistance turns around the tube; voltage regulator was used as a power supply to the test heated tube section. The AM4200 anemometer was used to measure the air velocity. Figure 1 illustrates the schematic diagram of the experimental setup. (For more information about the experimental setup, please see Ref. [8]).

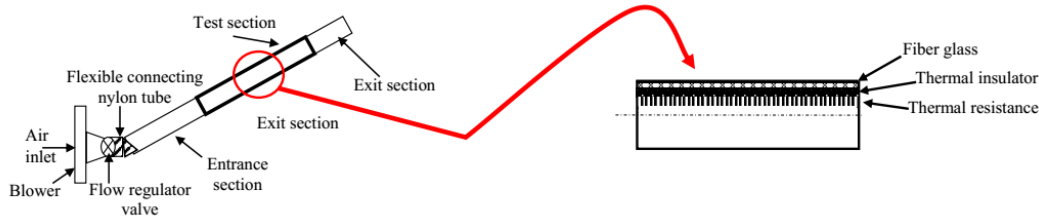


Fig.1. Schematics drawing of the experiment setup [14].

**2.Data reduction**

In the current experiment, the steady state is assumed. The air properties are evaluated using the following relations

that based on the temperature range.  $250K \leq 0.5(\overline{T}_{in} + \overline{T}_{out}) \leq 375K$  [15].

$$\begin{aligned} \rho_f &= 2.209 - 3.414 \times 10^{-3} \left( \frac{T_{in} + T_{out}}{2} \right), & \text{kg/m}^3 \\ c_{p_f} &= \left[ 9.848 + 6.76 \times 10^{-4} \left( \frac{T_{in} + T_{out}}{2} \right) \right] \times 10^2, & \text{J/(kg K)} \\ k_f &= \left[ 3.479 + 7.58 \times 10^{-2} \left( \frac{T_{in} + T_{out}}{2} \right) \right] \times 10^{-3}, & \text{W/(m K)} \\ \mu_f &= \left[ 4.475 + 4.564 \times 10^{-2} \left( \frac{T_{in} + T_{out}}{2} \right) \right] \times 10^{-6}, & \text{kg/(m s)} \end{aligned}$$

The porosity was taken about 0.3661, due to the absence of the regular arrangement of the porous media inside the tube compared with the calculated value using the Eq. (2) [2].

$$\varepsilon = 0.32 + \left[ 0.45 \times \left( \frac{dp}{d} \right) \right] \quad (2)$$

The value from Eq. (1) about 0.37. Therefore, the permeability could be found using Eq. (3) [17]:

$$K = \frac{\varepsilon^3 d_p^2}{175 \times (1 - \varepsilon)^2} \quad (3)$$

The local heat transfer coefficient could be evaluated as, follow:

$$h_z = \frac{q}{[T_s - \left( \frac{T_{in} + T_{out}}{2} \right)]_z} \quad (4)$$

and

$$q_w = \frac{q}{A_s} \quad (5)$$

where

$$A_s = \pi dl$$

$$q = \dot{m} C_{p,a} (T_{out} - T_{in}) \quad (5)$$

where the heat energy could be evaluated using the electrical power equation.

$$Q = I \times V \quad (6)$$

The efficiency of the converted electrical power could be calculated for the heat transfer rate as follow:

$$\zeta = \left( 1 - \frac{q}{Q} \right) \times 100 \quad (7)$$

The local Nusselt number is defined as:

$$Nu_z = \frac{h_z d}{k_{eff}} \quad (8)$$

where  $k_{eff}$  is the effective porous media thermal conductivity which was determined as [18]:

$$k_{eff} = \varepsilon k_f - (1 - \varepsilon) k_p \quad (9)$$

where  $k_f$  and  $k_p$  are the fluid and porous media thermal conductivity, respectively. Reynolds number was defined as [2]:

$$Re = \frac{\rho_f u d_p}{\mu_f (1 - \varepsilon)} \quad (10)$$

Peclet number is defined as:

$$Pe = Re Pr_f \quad (11)$$

Grashof number (Gr) and Rayleigh numbers (Ra) are defined via Eq. (12) [18]:

$$\left. \begin{aligned} Gr_d &= \frac{g \beta K q_w d^2}{\varepsilon k_{eff} \left( \frac{\mu_f}{\rho_f} \right)^2} \\ Ra &= Gr_d \times Pr_f \end{aligned} \right\} \quad (12)$$

where

$$\beta = \frac{2}{(T_{in} + T_{out})}$$

Richardson number (Ri) is defined as:

$$Ri = \frac{Gr_d}{Re^2} \quad (13)$$

#### 4. Artificial neural network modeling

ANNs are enlivened by the parallel design of a human cerebrum and dependent on the functioning of organic neural systems. They contain a progression of a numerical conditions that are utilized to recreate organic procedures, for example, learning and memory. Normal neurons get motions through neurotransmitters situated on the dendrites, or layer of the neuron. At the point when the receiving signs are sufficient (outperform a specific amount), the neuron is enacted and discharges a prompt through the axon. This prompt may be sent to another neurotransmitter and might energize different neurons [19]. In order to prove the objective of Nusselt number evaluation, the least-squares method is used to solve the problem of the installation of the nonlinear smaller squares curve. This method is also known as Levenberg–Marquardt algorithm (LMA) which was originally proposed in 1944 by Kenneth Levenberg [20] and reclaimed later by Marquardt [21]. This optimization technique combines Gauss-Newton and steepest descent approaches to converge to an optimal solution. Undoubtedly it is one of the effective feedforward neural networks learning algorithm. In addition, it acts gradually as a gradient ratio strategy when the parameters are too far from optimal and are increasingly working like Gauss-Newton when the parameters could be near the optimal solution [22] while avoiding the negative aspects of both techniques. Below the Levenberg Marquardt algorithm:

$$[J^T J + \lambda I] \delta = J^T (y - \hat{y}) \quad (14)$$

where  $J$  is the Jacobian,  $\lambda$  is the damping parameter,  $I$  is the identity matrix, and  $\delta$  is increment to estimated parameter vector  $\hat{y}$ . Adding Fletcher's modification to the aforementioned equation by substituting the identity matrix  $I$  with the diagonal matrix:

$$[J^T J + \lambda \text{diag}(J^T J)] \delta = J^T (y - \hat{y}) \quad (15)$$

In this study, the dataset consists of experimental data pairs (N) of an independent of average Nusselt number (Nu), and dependent variables of Prandtl number (Pr), axial distance (x), cylinder angle of inclination ( $\theta$ ), and heat flux (q). In ANN configurations, a two-layer frontal feeding network is represented with a hidden neurons and neurons with linear output in Figure 2. Consequently, to assess the legitimacy of the model, 320 randomized trial data were randomly assigned for training, verification and testing by 70%, 15% and 15%, respectively. Moreover, the trained network with Levenberg-Marquardt backpropagation algorithm created the fitting network. Ultimately, using atrial-and-error method, were three hidden neurons determined gain the optimal model performance and the least error rate.

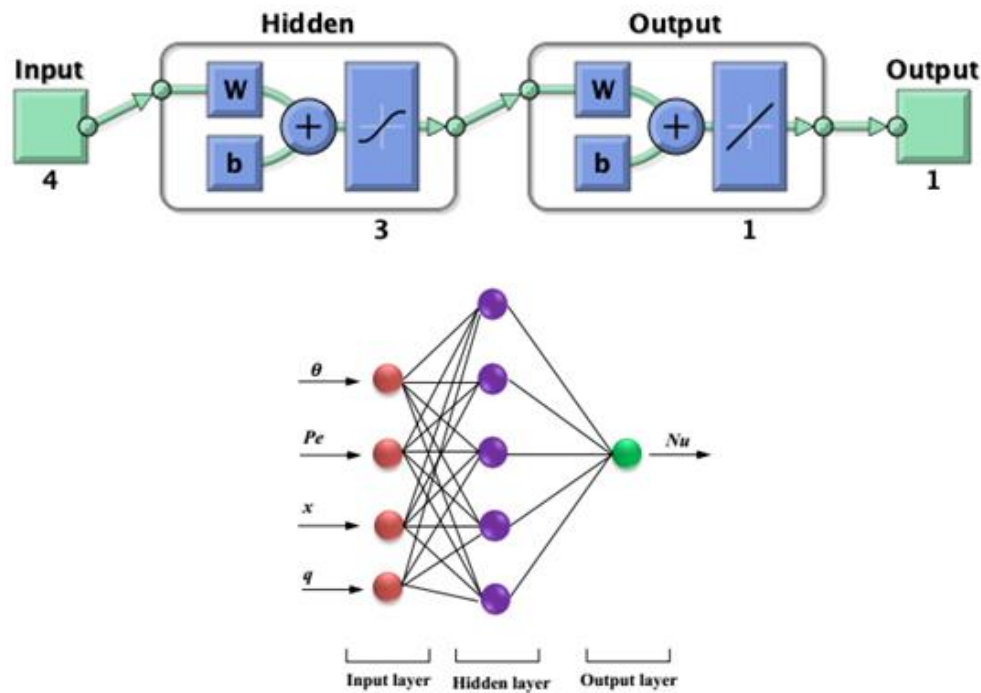
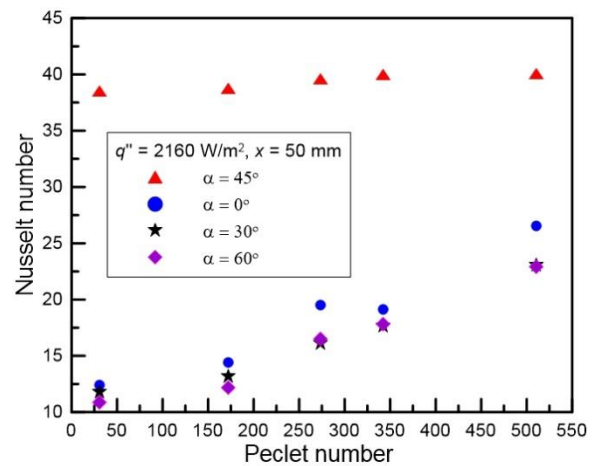
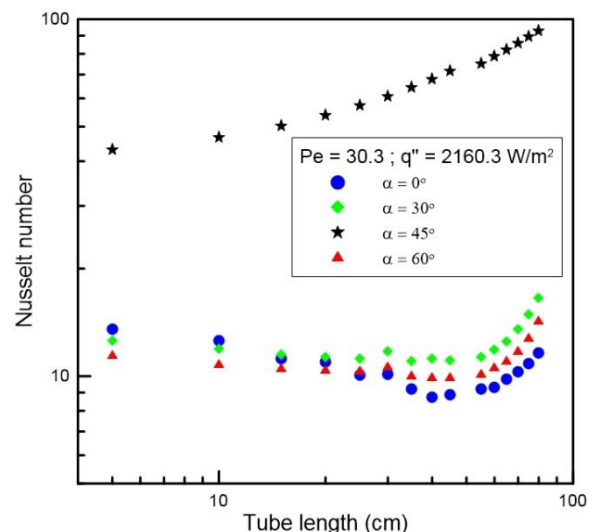


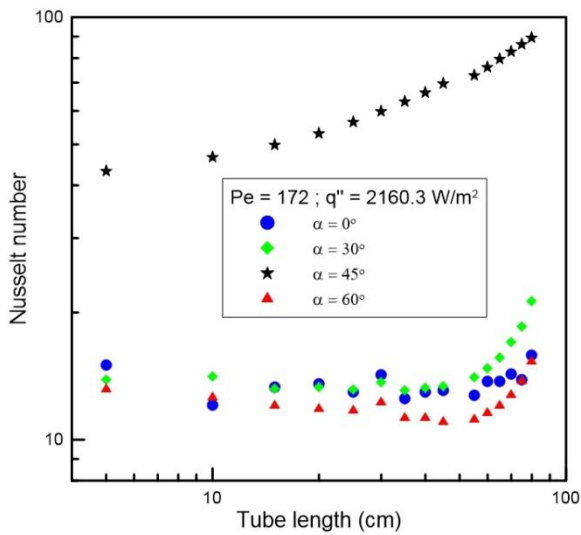
Fig. 2. Schematic of system models [13].

## 5.Result and Discussion

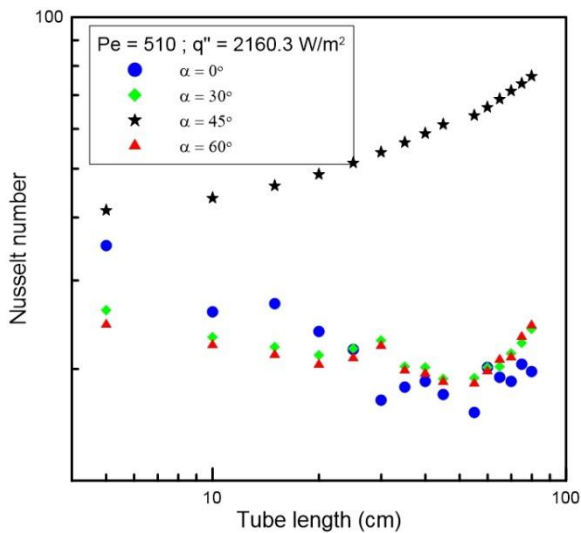
Fig.3 shows the effect of  $Pe$  number on the  $Nu$  number for the various inclined angles at a position of 50 mm and constant heat flow of  $2160 \text{ W/m}^2$ . In general, it is clear from this figure that the average Nusselt number increases with the increase of Peclet number in all the inclined angles. It can be seen that the largest Nusselt number is obtained at an inclination angle of  $45^\circ$  and its behavior corresponding to the Peclet number is different compared to the other cases, the result of the  $45^\circ$  angle, observed that the average number of Nusselt is not affected by the Peclet number as occurs in other angles. On another side, the distribution of the local Nusselt number has been examined along the tube for constant heat flux ( $2160 \text{ W/m}^2$  and change Peclet number from (30.3, 172, and 510) as shown in Figs. 4 to 6. From all these figures, it is clear that the local Nusselt number is increased along the tube length in the condition of angle  $45^\circ$ , while in the other conditions, the local Nusselt number behaving inversely to the tube length on the first half-length of the tube, because of thermal fully developed. As the length progresses, the average number of Nusselt increases rapidly. also, it was seen that the of local Nusselt number in the case of  $45^\circ$  is higher than other inclined angles and it was not affected by the change in Peclet number for the same heat flux quantity, while in other inclined angles, the local Nusselt number increases with the Peclet number increasing, though the heat flux was constant. The results were compared with a similar study [18]; there was a good match between them. Where  $n$  is the number of data points,  $Y_i$  represents the observed values, and  $\hat{Y}_i$  represents the predicted values.

Fig.3. The effect of Peclet number on Nusselt number different angles with  $q'' = 2160 \text{ W/m}^2$  and the  $x = 50\text{mm}$ .Fig. 4. The distribution of Nusselt number with tube length for  $Pe = 30.3$  and  $q'' = 2160 \text{ W/m}^2$





**Fig.5.** The distribution of Nusselt number with tube length for  $Pe = 172$  and  $q'' = 2160 \text{ W/m}^2$



**Fig.6.** The distribution of Nusselt number with tube length for  $Pe = 510$ , and  $q'' = 2160 \text{ W/m}^2$

The relative error and the mean relative error were respectively defined for each expected output by:

$$RE\% = \frac{|X_{Num} - X_{Pre}|}{X_{Num}} \times 100 \quad (16)$$

$$MRE\% = \frac{1}{N} \sum_{i=1}^N (RE\%)_i \quad (17)$$

where Num, Pre, and N are referring to the mean numerical values, expected values, and numeric data, respectively. To quantify the degree of the linear correlation between the observed and the predicted values the coefficient of determination is used. The general form for the determination coefficient ( $R^2$ ) equation is:

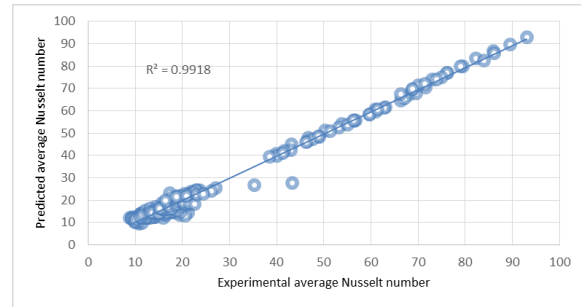
$$R^2 \equiv 1 - \frac{SS_{res}}{SS_{tot}} \quad (18)$$

where  $SS_{res}$  is squares sum of the residuals, and  $SS_{tot}$  is the total sum of the squares.

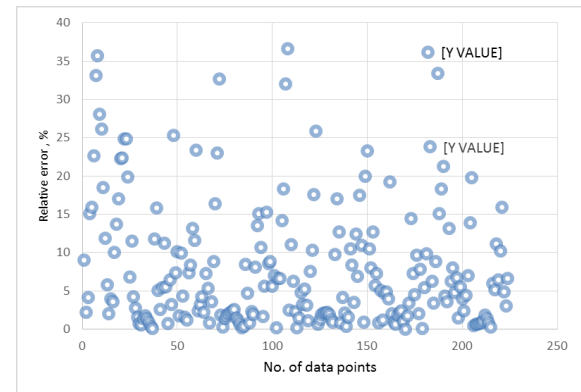
The mean squared error (MSE) is a risk function measure the average squared differences between the outputs and targets. Furthermore, it describes the proportion of the nature of an estimator. It is dependably non-negative and approaching closer to zero values are desirable. It is computed as:

$$MSE = \frac{1}{n} \sum_{i=1}^n (Y_i - \hat{Y}_i)^2 \quad (19)$$

The ANNs model for training data and average Nusselt number shown in Figs. 3 and 4. Where Fig.7 shows the compared between the experimental data with predicted data form ANNs model and Fig. 4 shows the relative error between the real data (experimental) and predicted data. It has been observed that to obtain a better AN gain order in this study, the average relative error is approximately 7.913%. The value of correlation coefficient ( $R^2$ ) about 99.18%, this value is best.

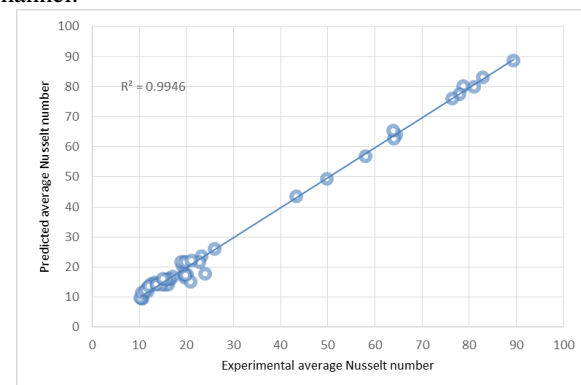


**Fig.7.** Predictions and Experimental of average Nu by ANNs with Training data.



**Fig. 8.** The relative error of the ANNs model for training data

Once, it was spotted from Figs. 9 and 10 for the testing data for the average Nusselt number. For best order for ANN and average Nusselt number, the mean relative error is 6.641%.and the coefficient of the equation, R-square is 99.46%, where it gives the best agreement between the experimental predictions data and ANNs. These results indicate that the ANNs model is suitable for predicting the heat transfer coefficient in the flow of the porous media channel.



**Fig.9.** Predictions and Experimental of average Nu by ANNs with testing data.

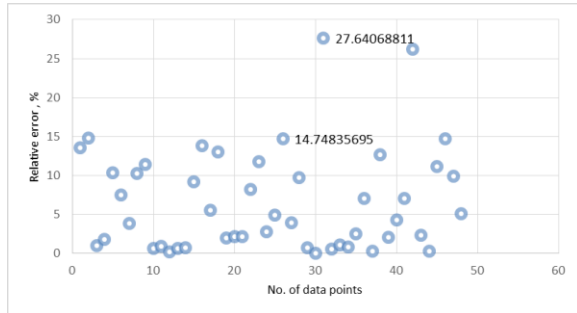


Fig. 10. The relative error of the ANNs model for testing data.

## 6. Conclusions

This paper includes a detailed experimental study on a mixed convection in circular horizontal tube and inclined with fitted porous media. The second part develop is the ANN model using the Nusselt number was estimated in this system. The ANN model has been shown to be used effectively to estimate heat transfer coefficient in airflow. The results of the study can be summarized as follows:

- Peclet number has a limited effect on average Nusselt and local numbers in case 45. Average Nusselt number was about 2, when Peclet number is changed from 30.3 to 510 for the heat flux 2160 W/m<sup>2</sup>, but the other slanted angle conditions were affected significantly by changing Peclet number.
- For the training data, the mean relative error about 7.913% and the R<sup>2</sup> is 99.18%.
- For the testing data, the mean relative error about 6.641% and the R<sup>2</sup> is 99.46%.
- Predicting the heat transfer coefficient with the ANN model gives a good compatibility with experimental value and has a lower error. Also, it is present that ANN is more credible for the modeling of such nonlinear systems.

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